# Gems of TCS 

## Secret Sharing

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November 15, 2023

## Treasure Map



## EXAMPLES

- Documents for a secret project


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- Documents for a secret project
- Missile launch codes


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## EXAMPLES

- Documents for a secret project
- Missile launch codes
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- Blockchains
- Internet Corporation for Assigned Names and Numbers (ICANN): Burkina Faso, Canada, Czech Republic, Trinidad and Tobego, China, USA, UK


## 2-OUT-OF-2 SECRET SHARING

- For secret message $m$, generate shares $s_{A}$ for Alice and $s_{B}$ for Bob


## 2-OUT-OF-2 SECRET ShARING

- For secret message $m$, generate shares $s_{A}$ for Alice and $s_{B}$ for Bob
- $s_{A}$ has no information about $m$


## 2-out-of-2 Secret Sharing

- For secret message $m$, generate shares $s_{A}$ for Alice and $s_{B}$ for Bob
- $s_{A}$ has no information about $m$
- $s_{B}$ has no information about $m$


## 2-OUT-OF-2 SECRET ShARING

- For secret message $m$, generate shares $s_{A}$ for Alice and $s_{B}$ for Bob
- $s_{A}$ has no information about $m$
- $s_{B}$ has no information about $m$
- $s_{A}$ and $s_{B}$ are sufficient to recover $m$


## $n-O U T-O F-n$ SECRET SHARING

- For secret message $m$, generate $n$ shares

$$
s_{1}, \ldots, s_{n}
$$

## $n-O U T-O F-n$ SECRET SHARING

- For secret message $m$, generate $n$ shares $s_{1}, \ldots, s_{n}$
- Each of n players gets their share


## $n$-OUT-OF-n SECRET SHARING

- For secret message m, generate $n$ shares $s_{1}, \ldots, s_{n}$
- Each of n players gets their share
- Every set of $n-1$ shares has no information about $m$


## $n$-OUT-OF-n SECRET SHARING

- For secret message m, generate $n$ shares $s_{1}, \ldots, s_{n}$
- Each of n players gets their share
- Every set of $n-1$ shares has no information about $m$
- Can recover $m$ from $s_{1}, \ldots, s_{n}$


## $k$-OUT-OF-n SECRET Sharing

- For secret message $m$, generate $n$ shares $S_{1}, \ldots, s_{n}$


## $k$-OUT-OF-n Secret Sharing

- For secret message m, generate $n$ shares $S_{1}, \ldots, S_{n}$
- Each of $n$ players gets their share


## k-OUT-OF-n SECRET Sharing

- For secret message m, generate $n$ shares $s_{1}, \ldots, s_{n}$
- Each of n players gets their share
- Every set of $k-1$ shares has no information about $m$


## $k$-OUT-OF-n SECRET Sharing

- For secret message m, generate $n$ shares $s_{1}, \ldots, s_{n}$
- Each of n players gets their share
- Every set of $k-1$ shares has no information about $m$
- Can recover $m$ from any set of $k$ shares


## General Secret Sharing

